Reinforcement learning of conditional computation policies for neural networks

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### **Motivation**

- Using RL to take decisions inside deep architectures
- Running high capacity models on low-end devices
  - Phones, mobile devices, electric wheelchair, etc.

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- Large networks, fast evaluation?
  - sparse models
  - pruning, quantization
  - lazy/conditional evaluations

## **Conditional Computation**

- Learn a gater function
  - $\rightarrow$  which parts of the model to evaluate

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- $\rightarrow$  which parts are useful
- Learn the main model concurrently

# Conditional Computation with RL

- Build model with parameters  $\theta$
- Divide parameters/computation into disjoint subsets of  $\theta/H$
- Learn a gating policy π<sub>ω</sub>(x) with separate parameters ω
  →stochastic policy with binary actions (on/off)
  →one action per subset
  →state space is x

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• Learn the main model( $\theta$ ) concurrently

#### The **REINFORCE** estimator

*k*-Bernoulli policy:

$$\sigma = \operatorname{sigm}(W^{(\omega)}\mathbf{x} + b^{(\omega)})$$

 $u_i \sim \text{Bern}(\sigma_i)$ 

$$\pi(\mathbf{u} \,|\, \mathbf{x}) = \prod_{i=1}^k \sigma_i^{u_i} (1 - \sigma_i)^{(1-u_i)}$$

$$\nabla_{\omega} \mathcal{L} = \sum_{j}^{minibatch} (cost(\mathbf{x}_j) - b) \nabla_{\omega} \log \pi_{\omega}(\mathbf{u}_j | \mathbf{x}_j)$$

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*b* is an exponential moving average of the costs.

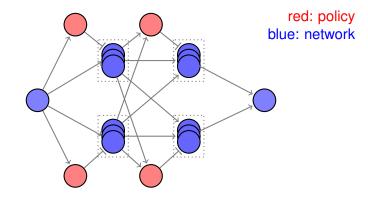
# **Policy Regularization**

• 
$$L_b = \sum_j^n \|\mathbb{E}\{\sigma_j\} - \tau\|_2$$
  
each unit is  $\tau$  in  $\mathbb{E}$  over the xs

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$$L_e = \mathbb{E}\{\|(\frac{1}{n}\sum_{j}^{n}\sigma_j) - \tau\|_2\}$$
  
the mean of units is  $\tau$  for some **x**

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## **Fully-Connected Architecture**

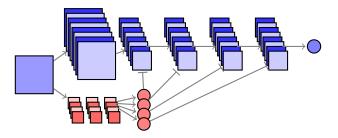


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## **Convolutional Architecture**

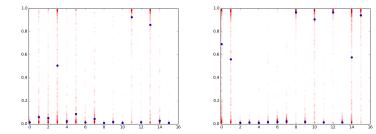
red: policy blue: network

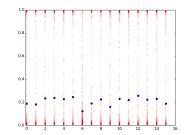
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All kinds of parametrizations are possible

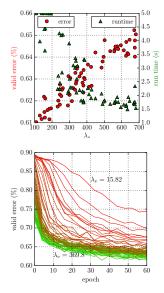
# Policies (fully connected, MNIST)





# **Policy Regularization**

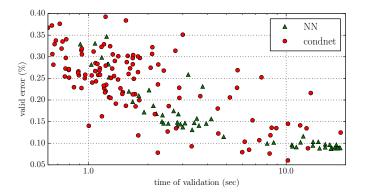
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the mean of units is  $\tau$  for some **x**



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## **Fully-Connected Results**

- MNIST, CIFAR-10, SVHN
- Same or better accuracy than conventional NN
- up to 5× faster
- >25-50× less computations



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### **Convnet Results**

model	test error	Ν	au	test time
conv-condnet	.157	4	0.5	1.03s
conv-condnet	.167	4	0.3	0.84s
conv-condnet	.176	4	0.2	0.66s
conv-condnet	.173	2	0.5	0.58s
conv-NN	.159	4	-	1.07s

CIFAR-10 results for conditional convnets

### Conclusion

#### It works!

- Similar accuracy, lower forward-pass time
- Much less computations being done (25% active nodes → ~6.25% computations, 10%→1%)

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- Does not scale very well (REINFORCE?)
- Hard to compete with dense computations
- Chicken and egg problem during learning